

*What Shifts the Beveridge Curve?*  
*Recruiting Intensity and Financial Shocks*

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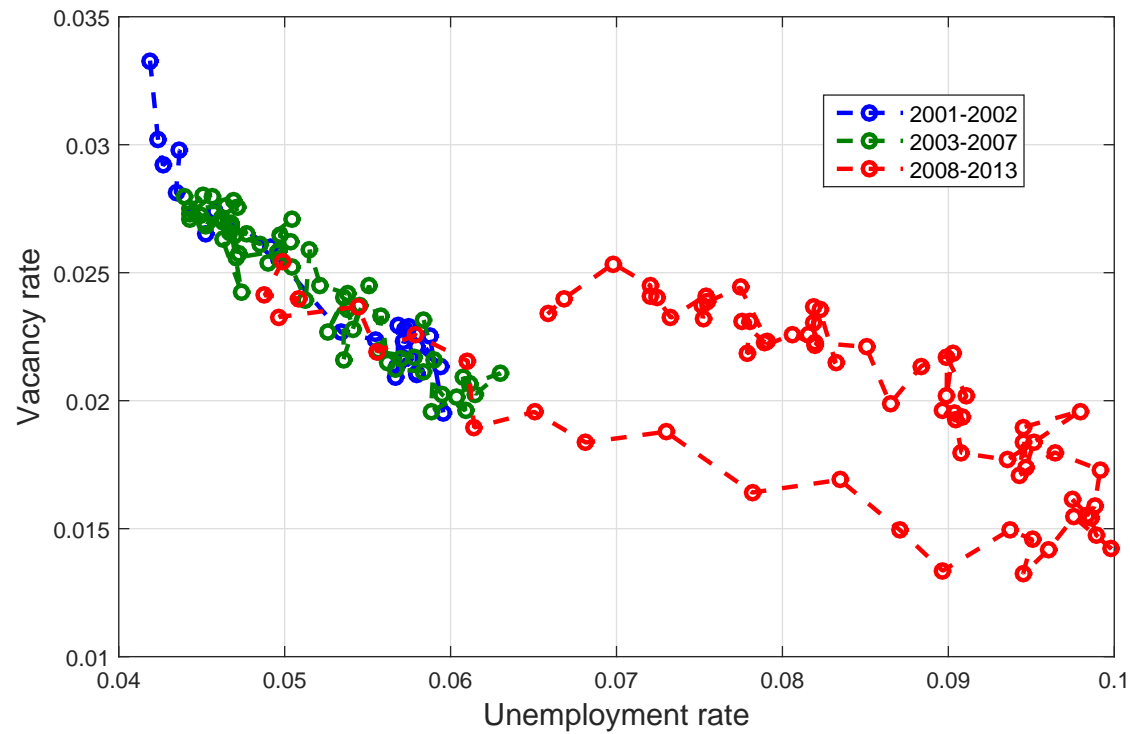
New York University

**Gianluca Violante**

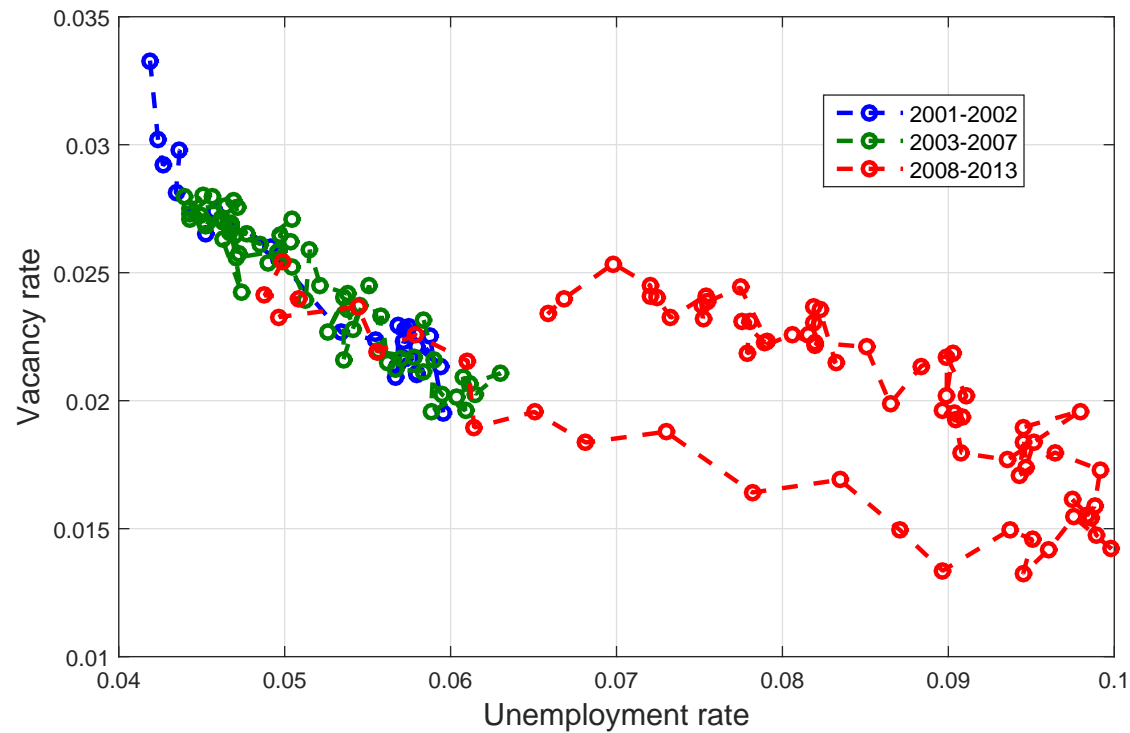
New York University

RBA Quantitative Macroeconomics Workshop

# The outward shift in the Beveridge curve



# The outward shift in the Beveridge curve



It indicates a deterioration in **aggregate matching efficiency**  $\Phi_t$

$$H_t = \Phi_t V_t^\alpha U_t^{1-\alpha}$$

# MEASUREMENT OF $\Phi_t$

# Estimating $\Phi_t$ accounting for compositional changes

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- Hall and Schulhofer-Wohl → among job-seekers, include
  - ▶ Nonparticipants ( $N_t$ )
  - ▶ Employed ( $E_t$ )

$$H_t = \Phi_t \cdot \underbrace{\left( 1 + s_t^N \frac{N_t}{U_t} + s_t^E \frac{E_t}{U_t} \right)}_{\text{composition factor}}^{1-\alpha} \cdot V_t^\alpha U^{1-\alpha}$$

- Veracierto → estimate  $(s_t^N, s_t^E)$  through data on worker flows

## Estimating $\Phi_t$ accounting for compositional changes

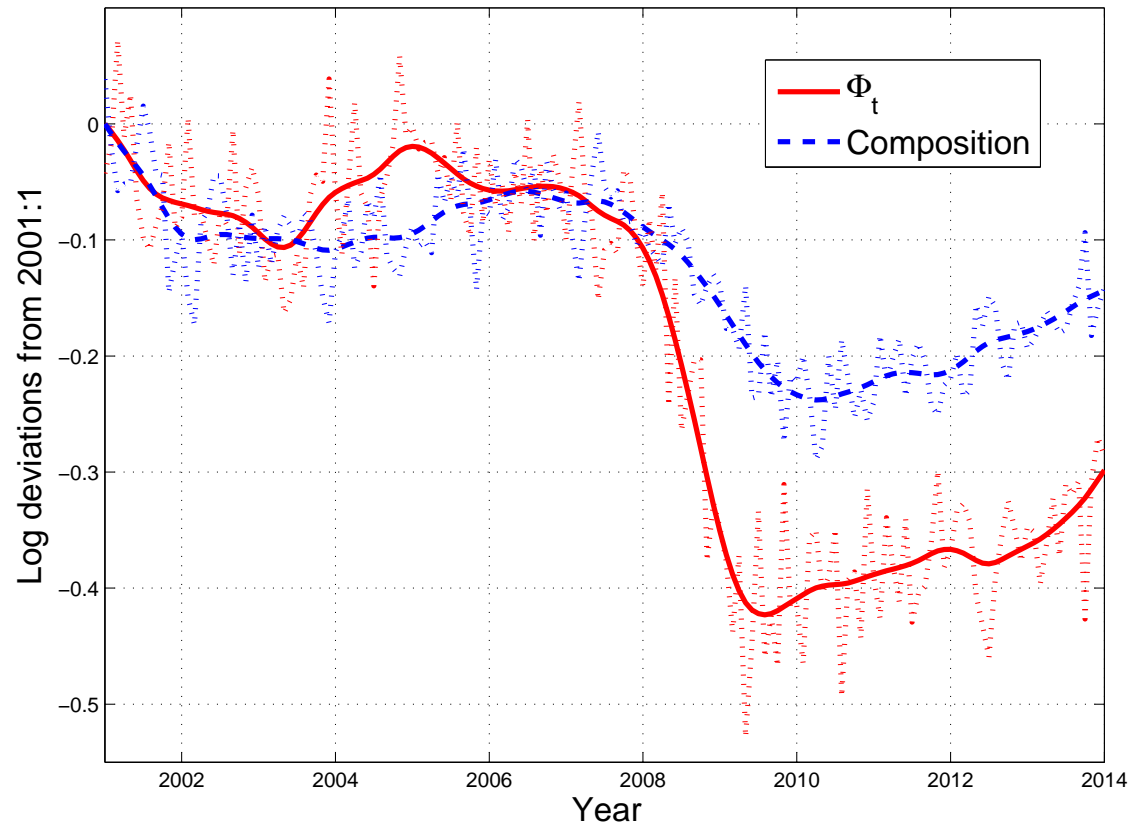
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- Veracierto → estimate  $(s_t^N, s_t^E)$  through data on worker flows
- Fujita and Moscarini → exclude workers on temporary layoff from the matching function
- Fix  $\alpha = 0.5$ , compute composition factor, and get  $\Phi_t$  as a residual

# Measured drop in aggregate matching efficiency



2001: -10 percent & fast rebound

2007-09: -30 percent & slow recovery



# Explaining the deterioration in matching efficiency

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$$H_t = \Phi_t V_t^\alpha U_t^{1-\alpha}$$

## 1. Mismatch ↑

- ▶ Sahin-Song-Topa-Violante 2014; Elsby-Michaels-Ratner 2014

## 2. Worker's search effort ↓

- ▶ Mukoyama-Patterson-Sahin 2014; Hagedorn-Karahan-Manovskii-Mitman 2014

## 3. Firm's recruiting intensity ↓

- ▶ Davis-Faberman-Haltiwanger 2012; Kaas-Kircher 2014

# Firms' recruiting intensity

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- Effective vacancies:

$$V_t^* = \int e_{it} v_{it} di$$

- $v_{it}$ : max open positions ready to be staffed and costly to create
- $e_{it} \in [0, 1]$ : probability of filling an open position —an outcome of how much firms choose to spend on recruitment activities
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- Aggregate matching function:

$$H_t = (V_t^*)^\alpha U_t^{1-\alpha} = \Phi_t \cdot V_t^\alpha U_t^{1-\alpha} \quad \text{with} \quad \Phi_t = \left[ \int e_{it} \left( \frac{v_{it}}{V_t} \right) di \right]^\alpha$$

# MECHANISM

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  - ▶ Haltiwanger-Jarmin-Miranda 2014

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  - ▶ Recruiting intensity  $\Phi_t = \left[ \int e_{it} \left( \frac{v_{it}}{V_t} \right) di \right]^\alpha$  falls
- **TFP shock:** more neutral across firms, so smaller effect on  $\Phi_t$

# ECONOMIC ENVIRONMENT

RANDOM-MATCHING MODEL WITH MULTI-WORKER FIRMS

COOPER-HALTIWANGER-WILLIS 07, ELSBY-MICHAELS 13, ACEMOGLU-HAWKINS 14

# Cast of characters

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## 1. Firms

- Operate a DRS technology  $y(z, n)$ ,  $z$  stochastic
- Hire in frictional labor markets: choose  $(e, v)$
- Face non-negative dividend constraint  $\rightarrow$  borrowing
- Endogenous entry and exit/default
  - ▶ Sedlacek 14; Siemer 14; Schott 14

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## 2. Banks

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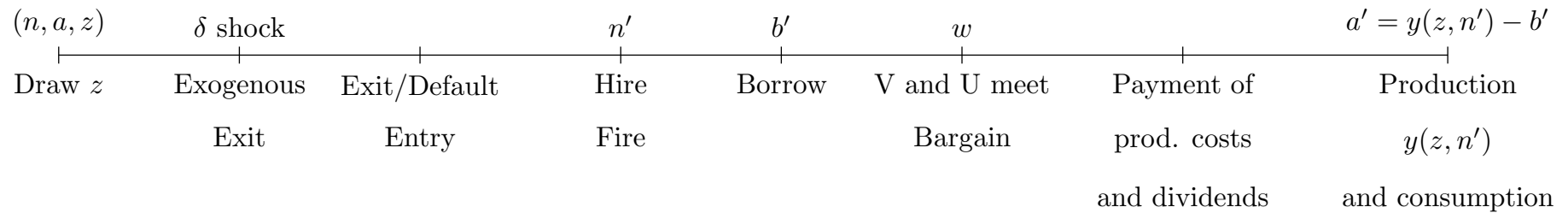
## 2. Banks

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## 3. Households

- Risk neutral representative family (some members unempl.)
- Save into bank deposits and mutual fund that owns all firms

# Timeline



Individual firm's state variables:

- $n$ : initial employment (pre-hiring)
- $a$ : initial net worth
- $z$ : productivity

## Entry, exit, hire/fire decisions

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- **Entry decision:**  $\lambda_0$  potential entrants drawing  $z \sim \Gamma_0(z)$ 
  - ▶ **fraction  $\varepsilon$  of start-up cost  $\chi_0$  financed by equity**

$$-\varepsilon\chi_0 + \mathbb{V}^i(0, -(1 - \varepsilon)\chi_0, z^*) = 0$$



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- **Stay as incumbent (and repay) or exit-repay or exit-default**

$$\mathbb{V}(n, a, z) = \max \{ \mathbb{V}^i(n, a, z), a, 0 \}$$

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- **Incumbent: fire or hire**

$$\mathbb{V}^i(n, a, z) = \max \{ \mathbb{V}^f(n, a, z), \mathbb{V}^h(n, a, z) \}$$

## Incumbent firms' decisions: fire

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$$\mathbb{V}^f(n, a, z) = \max_{n', b'} d^f + \beta(1 - \delta) \sum_{z' \in \mathcal{Z}} \mathbb{V}(n', a', z') \Gamma(z', z)$$

*s.t.*

$$n' \leq n$$

$$d^f \equiv a - w(z, n', b')n' - \chi + Q(n', b', z)b' \geq 0$$

$$a' = y(z, n') - b'$$

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Note: wage determined by Nash bargaining (Stole-Zwiebel solution)

## Incumbent firms' decisions: hire

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$$\mathbb{V}^h(n, a, z) = \max_{e \in [0,1], v > 0, b'} d^h + \beta(1 - \delta) \sum_{z' \in \mathcal{Z}} \mathbb{V}(n', a', z') \Gamma(z', z)$$

*s.t.*

$$n' - n = q(\theta^*)ev$$

$$d^h \equiv a - w(z, n', b')n' - \chi - C(e, v, n) + Q(n', b', z)b' \geq 0$$

$$a' = y(z, n') - b'$$

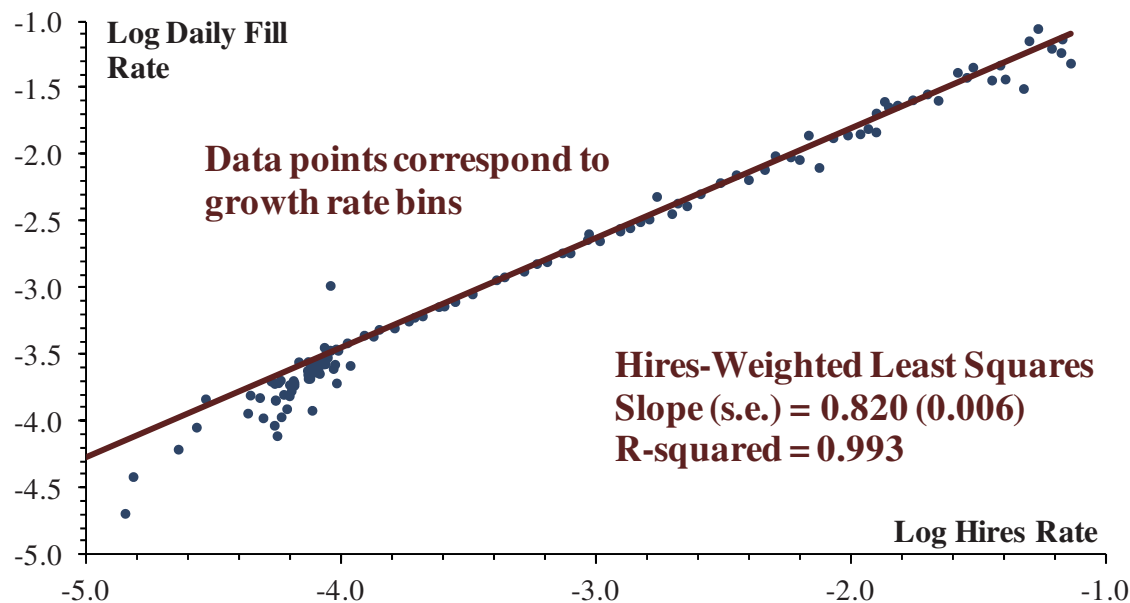
## Choice of functional form for $C(e, v, n)$

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DFH: Log-linear relation btw job-filling rate  $q(\theta^*)e$  and growth rate

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DFH: Log-linear relation btw job-filling rate  $q(\theta^*)e$  and growth rate



Reverse engineer  $C(\cdot)$  that yields the above relationship

## Hiring problem

---

1. **Stage I:** Choose target employment level  $n' > n$
2. **Stage II:** Choose max new positions  $v$ , and recruitment effort  $e$



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$$C^*(n, n') = \min_{e \in [0, 1], v > 0} \left[ \frac{\kappa_1}{\gamma_1} e^{\gamma_1} + \frac{\kappa_2}{\gamma_2 + 1} \left( \frac{v}{n} \right)^{\gamma_2} \right] v$$

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*s.t.*

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- The solution yields the **job filling-rate**:

$$\log \left( \frac{h}{v} \right) \equiv q(\theta^*)e = \Omega(\kappa_1, \kappa_2, \theta^*) + \frac{\gamma_2}{\gamma_1 + \gamma_2} \log \left( \frac{n' - n}{n} \right)$$

## Why is recruiting effort increasing in the growth rate?

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$$\frac{n' - n}{n} = q(\theta^*) \cdot e \cdot \left(\frac{v}{n}\right)$$

1.  $e$  and  $v/n$  are both **inputs** in the production of employment growth

$$\frac{C}{v} = \left[ \frac{\kappa_1}{\gamma_1} e^{\gamma_1} + \frac{\kappa_2}{\gamma_2 + 1} \left(\frac{v}{n}\right)^{\gamma_2} \right]$$

2. cost of creating a new position is **increasing in both  $e$  and  $v/n$**
3. **relative curvature** of cost function  $C$  with respect to  $e$  and  $v/n$  determines their elasticity with respect to the desired growth rate

# Banks

---

- Competitive sector with free entry
- Intermediate funds at cost  $\varphi > 0$  (financial wedge)
- Pay risk-free return  $\bar{Q}^{-1} = \beta^{-1}$  on deposits
- Upon firm's default, i.e.,  $x^D(n', a', z') = 1$ , recover nothing

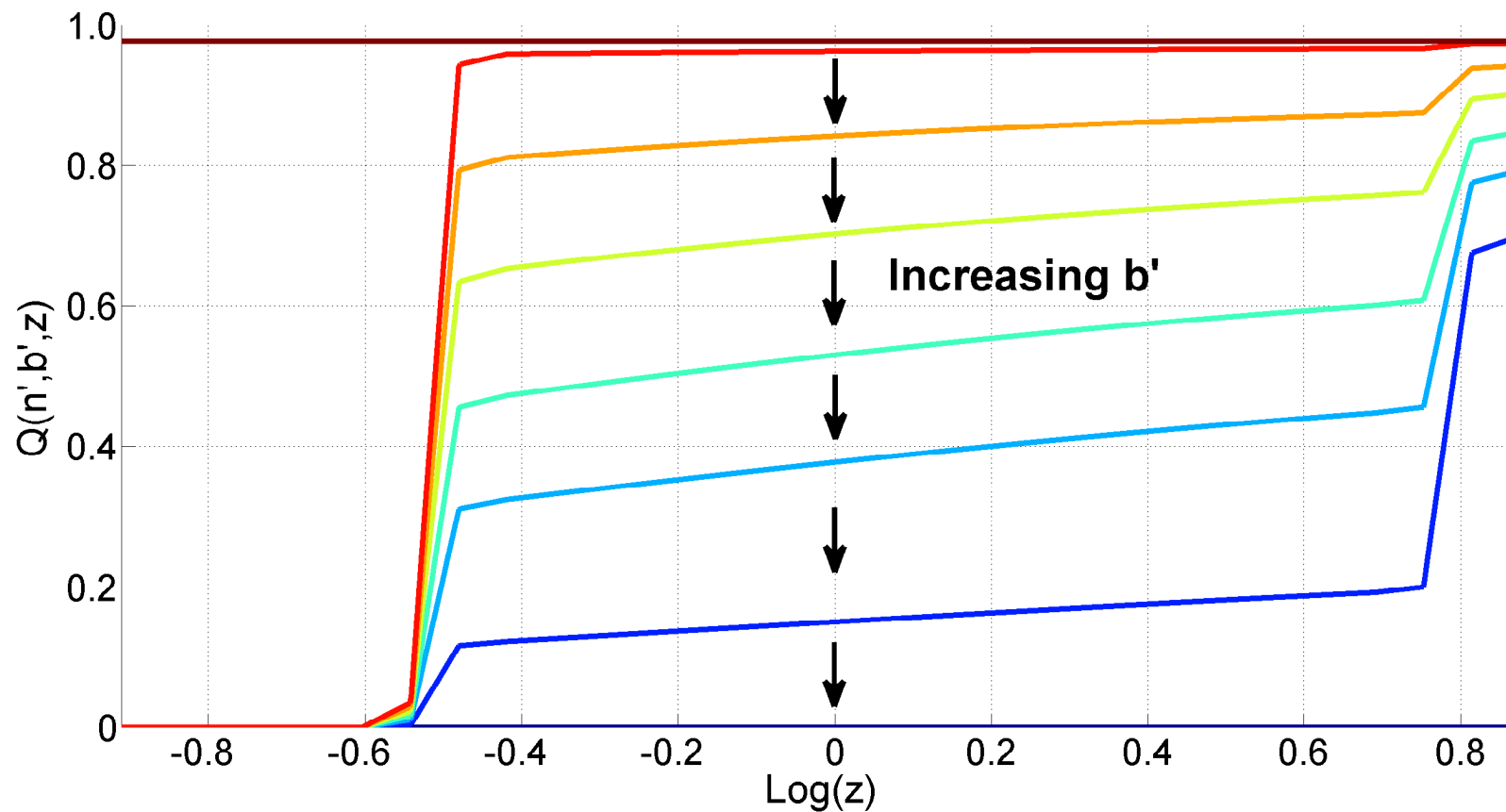
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- Upon firm's default, i.e.,  $x^D(n', a', z') = 1$ , recover nothing
- **Equilibrium price** of a loan to a firm of type  $(n', b', z)$ :

$$Q(n', b', z) = \bar{Q}(1 - \varphi)(1 - \delta) \left[ 1 - \sum_{z' \in \mathcal{Z}} x^D(\cdot) \Gamma(z', z) \right]$$

# (Inverse of) price of debt for start-ups



# Representative household

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$$\mathbb{W}(U, T, M) = \max_{M', T'} C + \beta \mathbb{W}(U', T', M')$$

*s.t.*

$$C + \bar{Q}M' + PT' = \int w(z, n', b')n'd\lambda + \omega U + (D + P)M + T$$

$$U' = U + \delta(1 - U) - \Phi V^\alpha U^{1-\alpha}$$

- $T$ : household deposits
- $M$ : shares of the mutual fund owning all firms
- $D$ : average dividends paid by firms

PRELIMINARY

PARAMETERIZATION



## Externally calibrated

Parameter		Value	Target
Discount factor (monthly)	$\beta$	0.9967	Risk-free rate
Potential entrants	$\lambda_0$	0.02	Meas. of incumbents = 1
Size of labor force	$\Lambda$	18.7	Average firm size = 17.5
Nash bargaining share of workers	$\eta$	0.5	—
Elasticity of matching function wrt $V_t$	$\alpha$	0.5	Empirical estimates
Financial intermediation wedge (monthly)	$\varphi$	0.002	Excess bond premium
External equity share of start-up cost	$\varepsilon$	0.50	Kauffman Firm Survey

Model period is 1 month

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Addition to the model: heterogeneity in DRS across firms

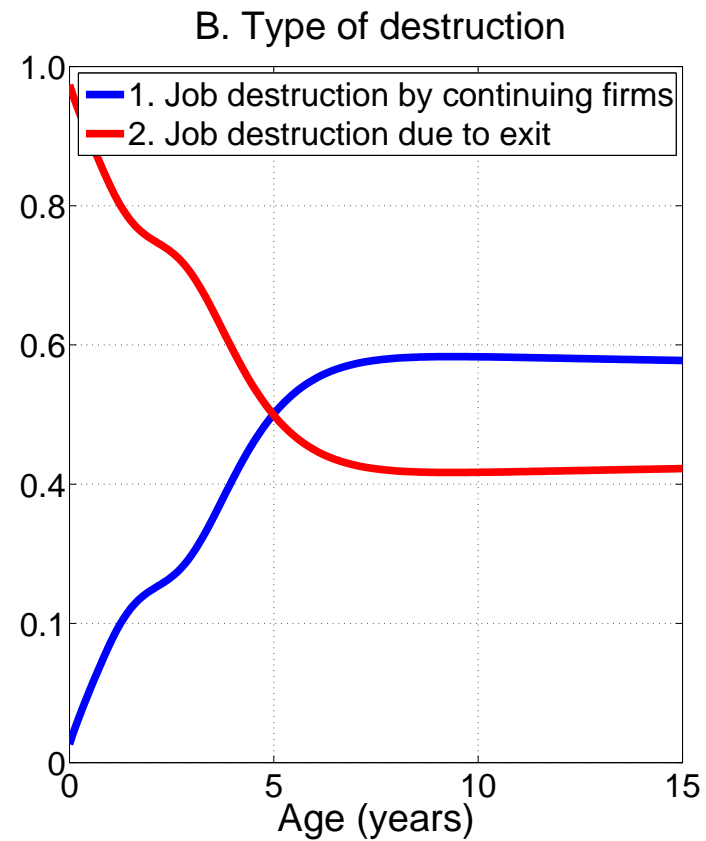
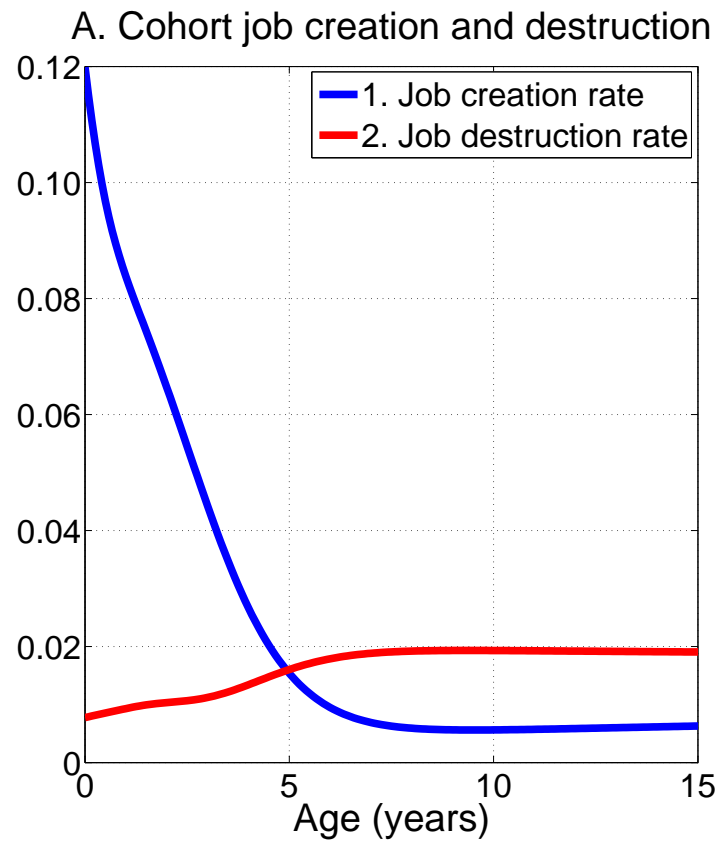
# Internally calibrated

Parameter		Value	Target	Model	Data
Flow of home production	$\omega$	0.62	Monthly separ. rate	0.03	0.02
Scaling of match. funct.	$\bar{\Phi}$	0.42	Monthly job finding rate	0.40	0.30
Midpoint DRS in prod.	$\nu$	0.70	Dividend share	0.06	0.05
High-Low DRS in prod.	$\Delta\nu$	0.20	Empl. share 500+	0.25	0.47
Persistence of $z$ shocks	$\Gamma$	0.99	Annual $ g  < 0.05$	0.50	0.42
SD of $z$ shocks	$\Gamma$	0.11	$SD(g)$	0.32	0.42
Cost elasticity wrt $e$	$\gamma_1$	3.74	Recr. int. small/large firms	1.23	1.50
Cost elasticity wrt $v$	$\gamma_2$	22.97	Elasticity of job. fill rate wrt $g$	0.86	0.82
Cost shifter wrt $e$	$\kappa_1$	4.88	Hiring cost/monthly wage	0.03	0.15
Cost shifter wrt $v$	$\kappa_2$	0.08	Vac. share. of small firms	0.18	0.34
Entry cost	$\chi_0$	0.28	Annual entry rate	0.09	0.11
(Exponential) distrib. of $z_0$	$\xi$	11.82	Share of JC by entrants	0.33	0.32
Operating cost	$\chi$	0.08	Survive $\geq 5$ years	0.62	0.50
Exogenous exit shock	$\delta$	0.008	Share of JD by exit	0.24	0.35

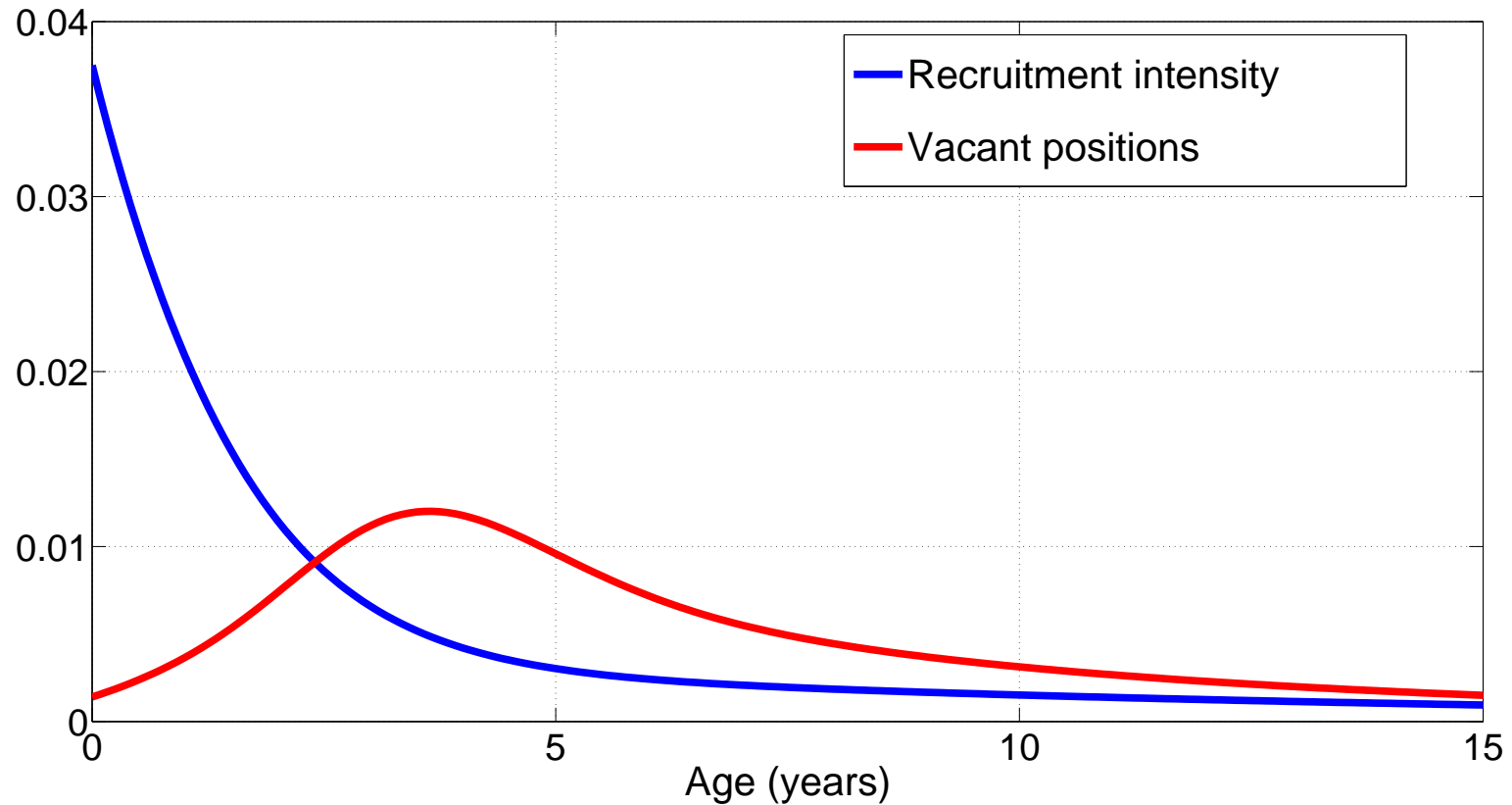
# “Up or out” dynamics of young firms

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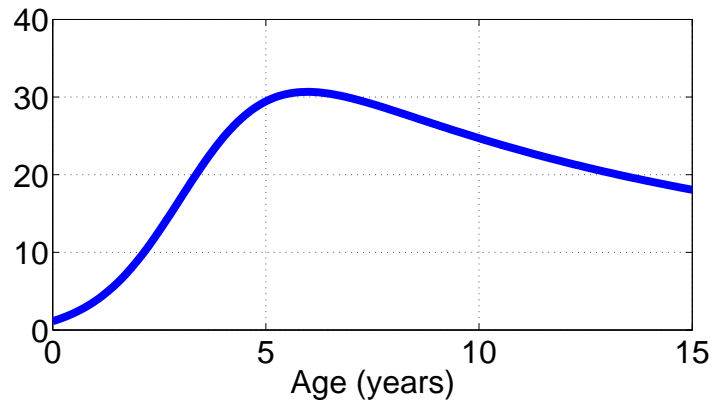
# Age distribution of recruiting intensity and vacancies



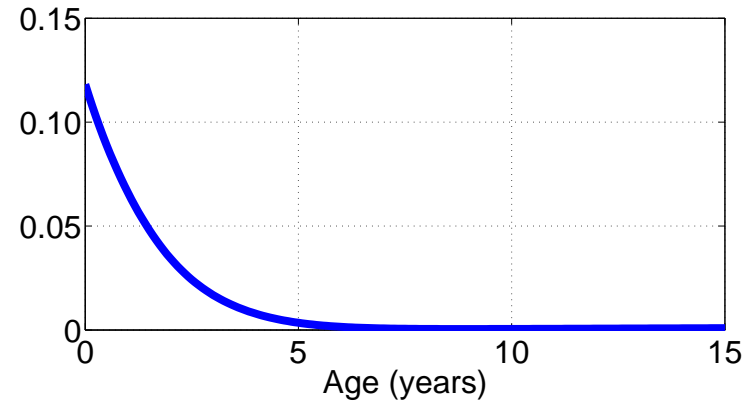
# Firms' life-cycle (averages)

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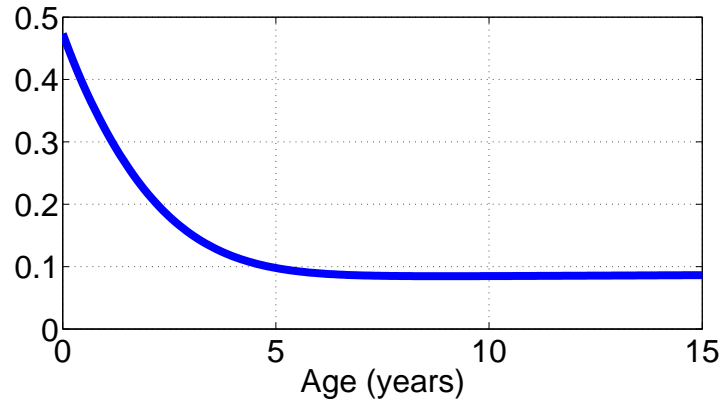
A. Size



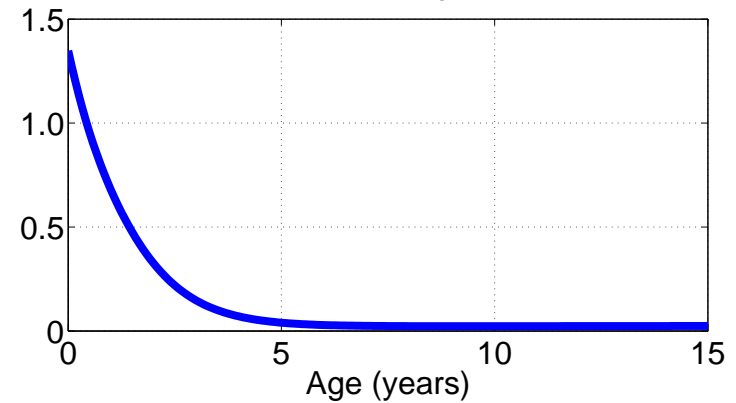
B. Growth Rate



C. Recruitment Effort



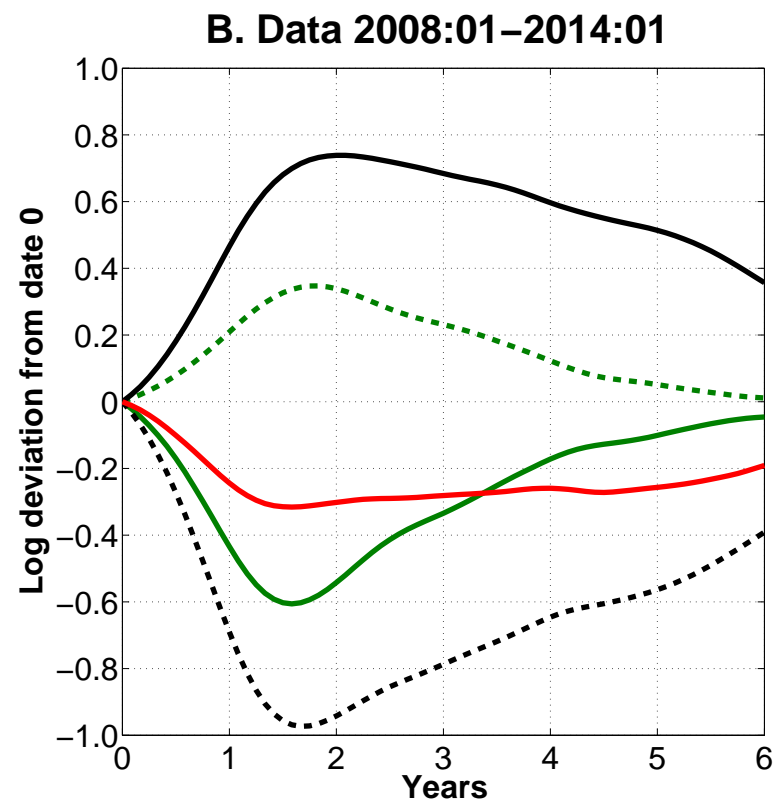
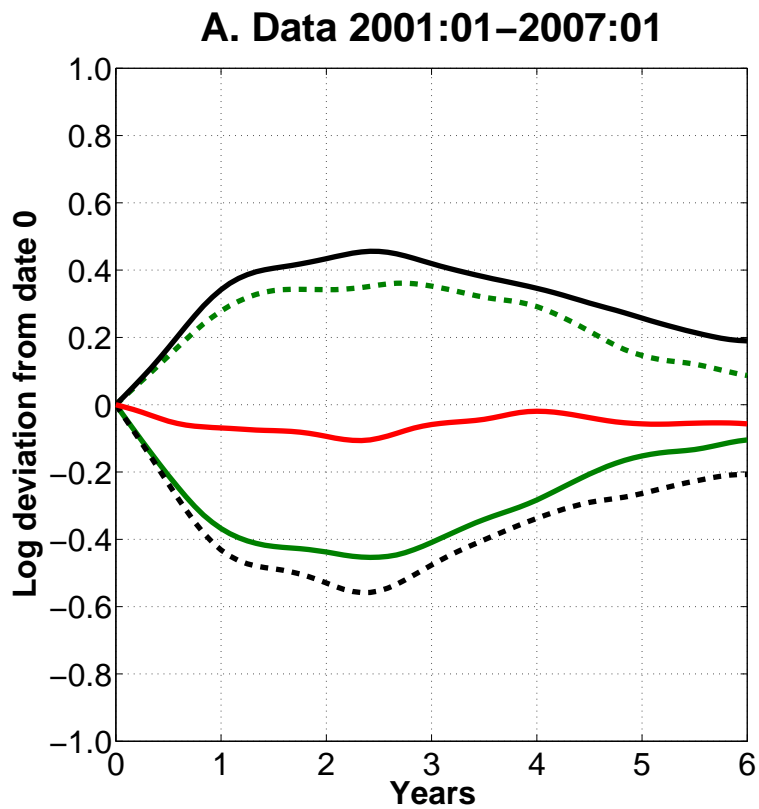
D. Debt to Output Ratio



# DATA TO BE EXPLAINED



# Data: 2001 vs 2008



— Vacancies    - - - Vacancy yield    — Unemployment    - - - Job finding rate    — Aggregate Recruitment Intensity

# EXPERIMENTS

# Experiments

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Trace **transitional dynamics** of the economy in response to:

- 2001 recession
  - ▶ Aggregate productivity  $Z$  ↓ by 4% and recovers in 6 years

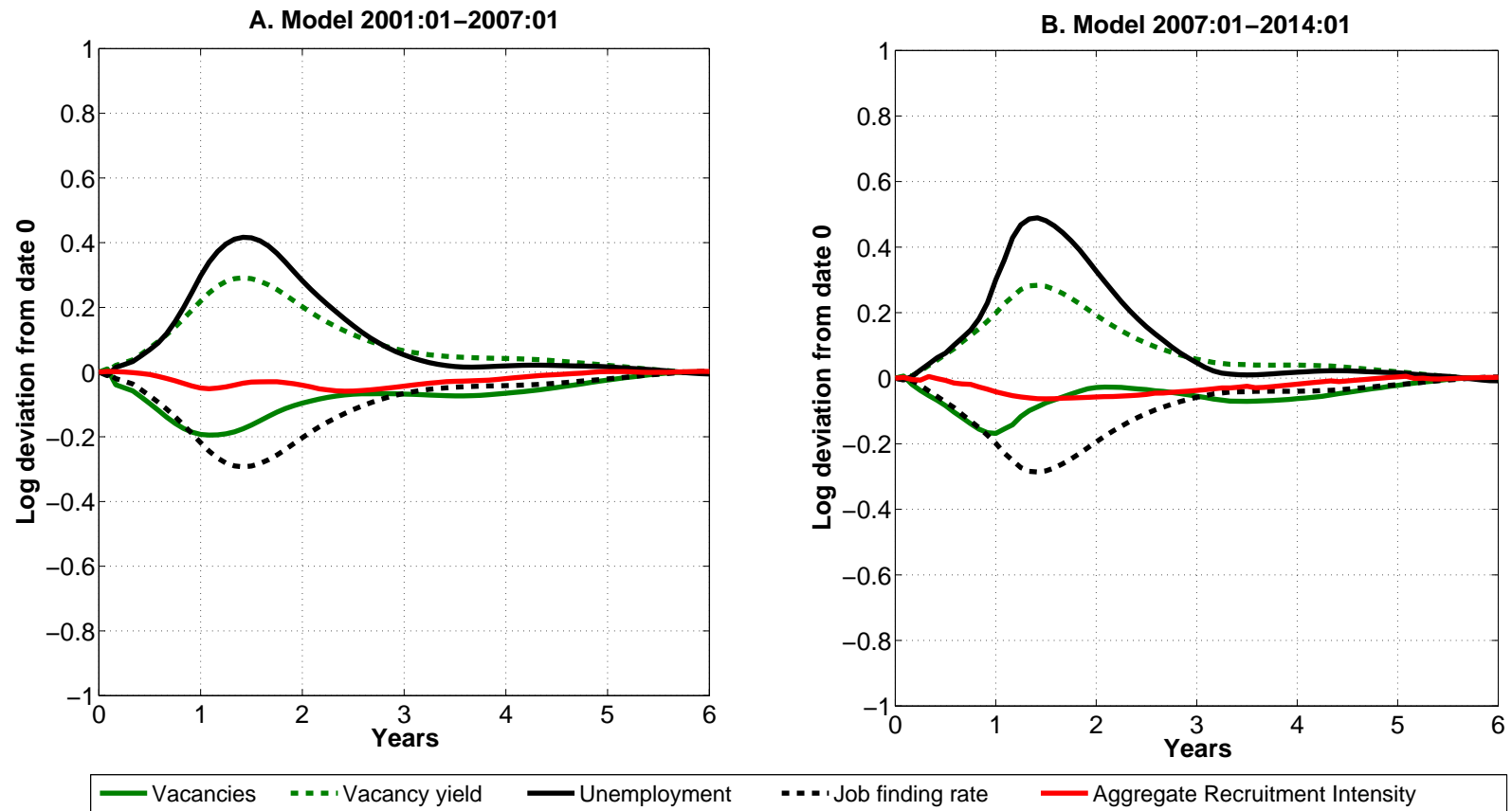
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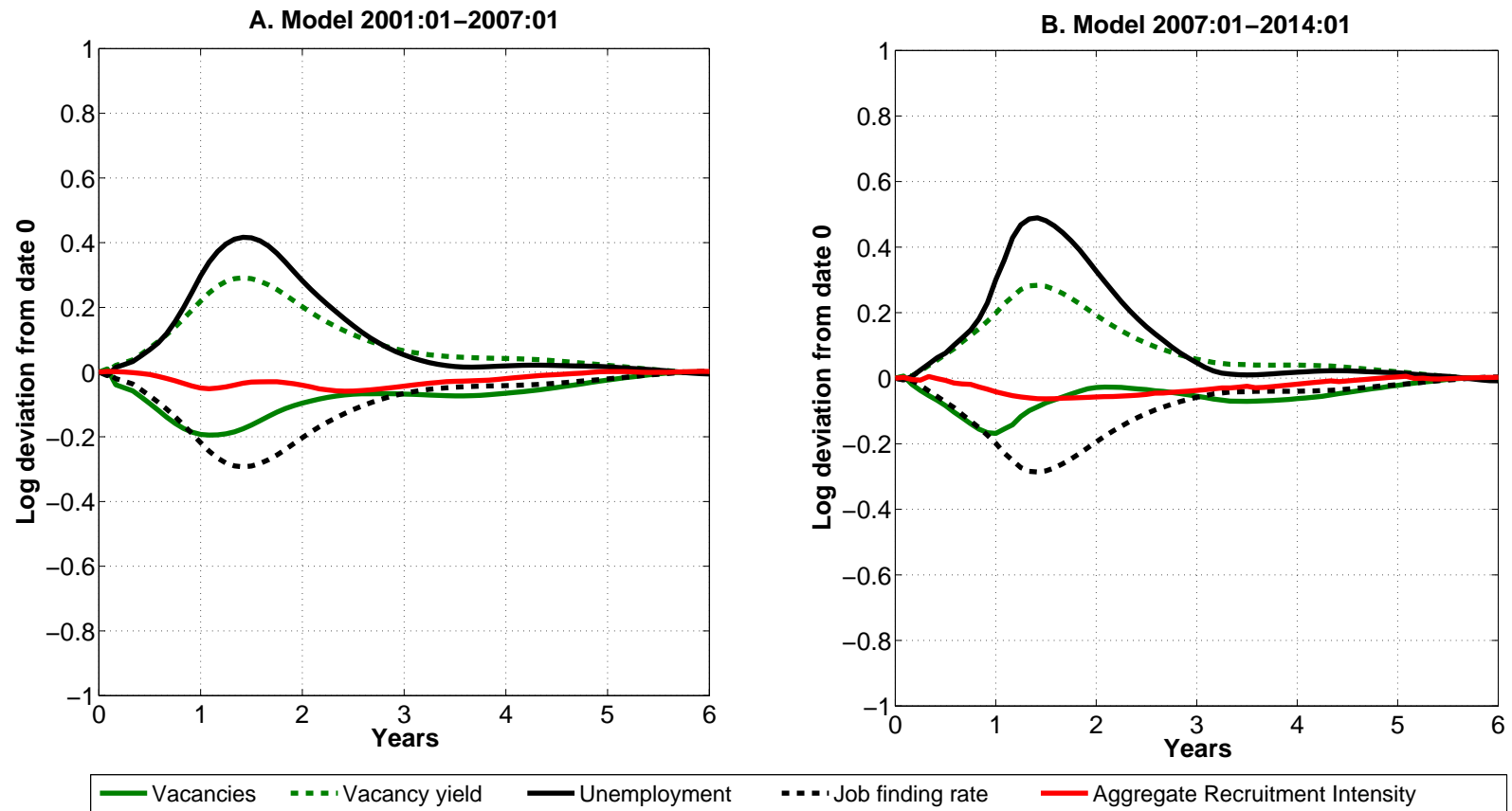
- 2001 recession
  - ▶ Aggregate productivity  $Z \downarrow$  by 4% and recovers in 6 years
- 2007-09 recession
  - ▶ Same aggregate productivity  $Z \downarrow$  combined with:
    - ▶ Financial shock
      - Financial wedge  $\varphi \uparrow$  and recovers in 6 years
      - Initial equity at start-up  $\varepsilon \downarrow$  and recovers in 6 years

# Model: 2001 vs. 2008



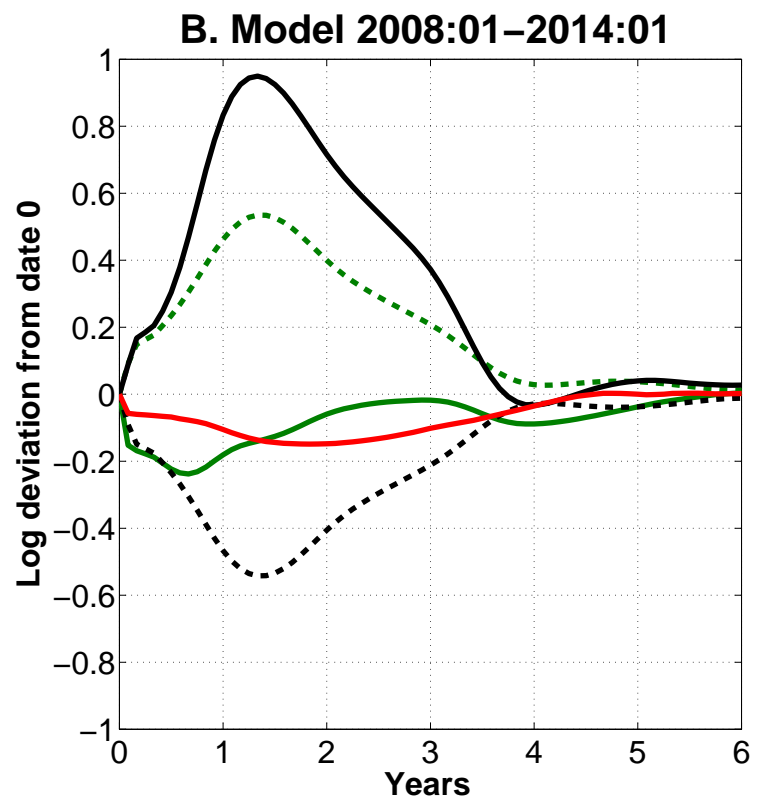
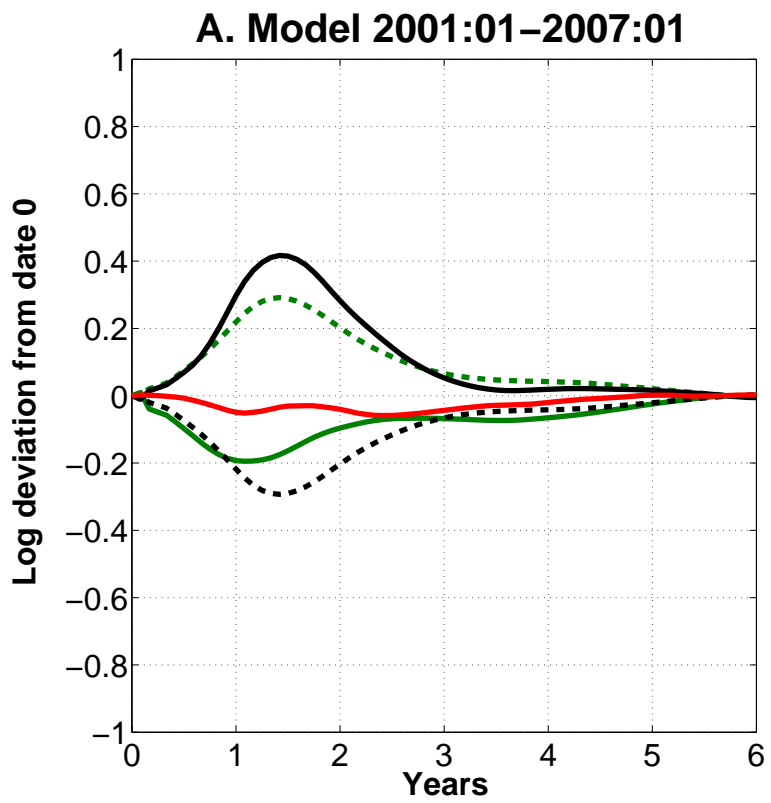
A: TFP Shock

# Model: 2001 vs. 2008



B: TFP Shock + increase in intermediation wedge  $\varphi$

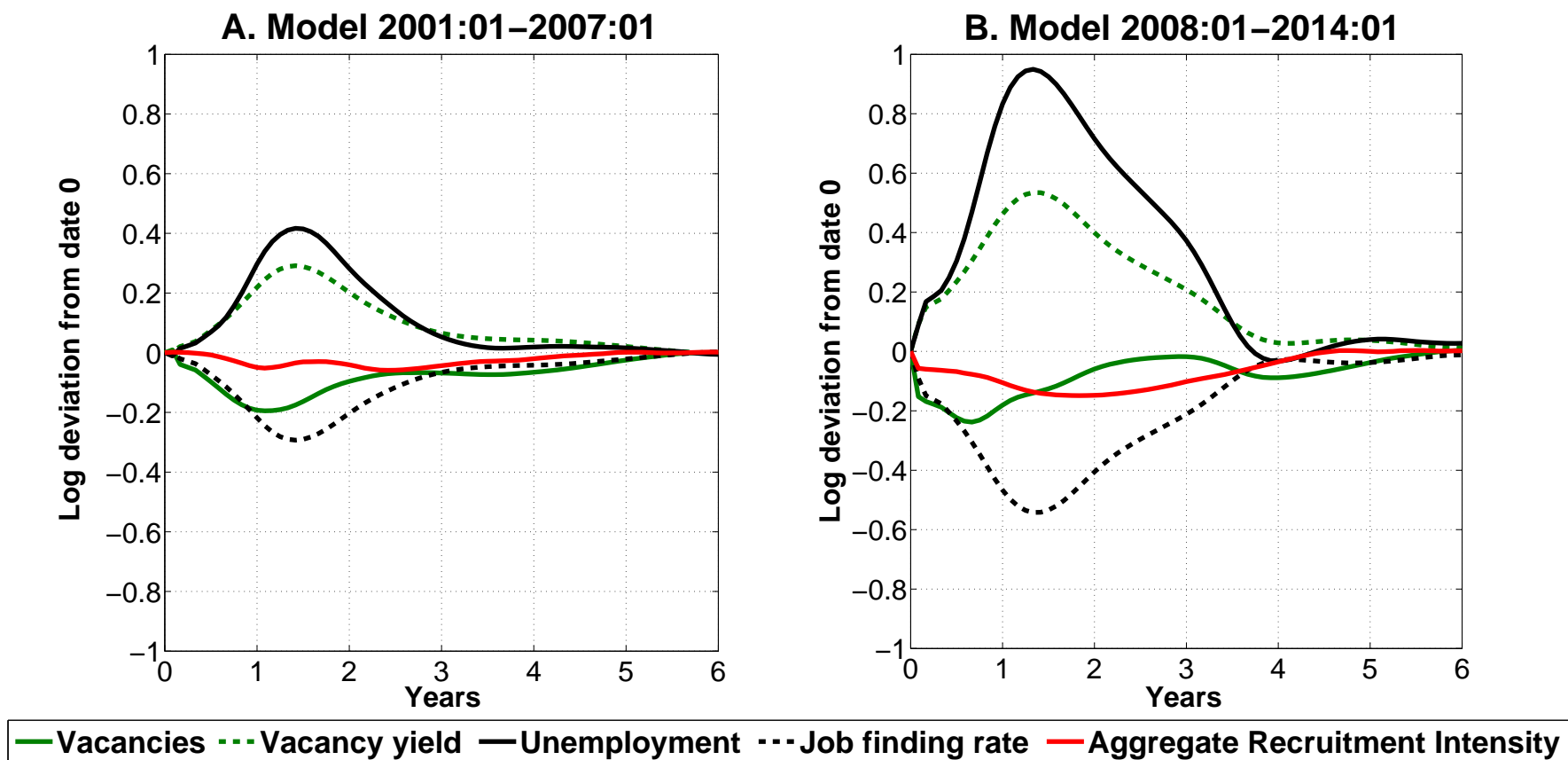
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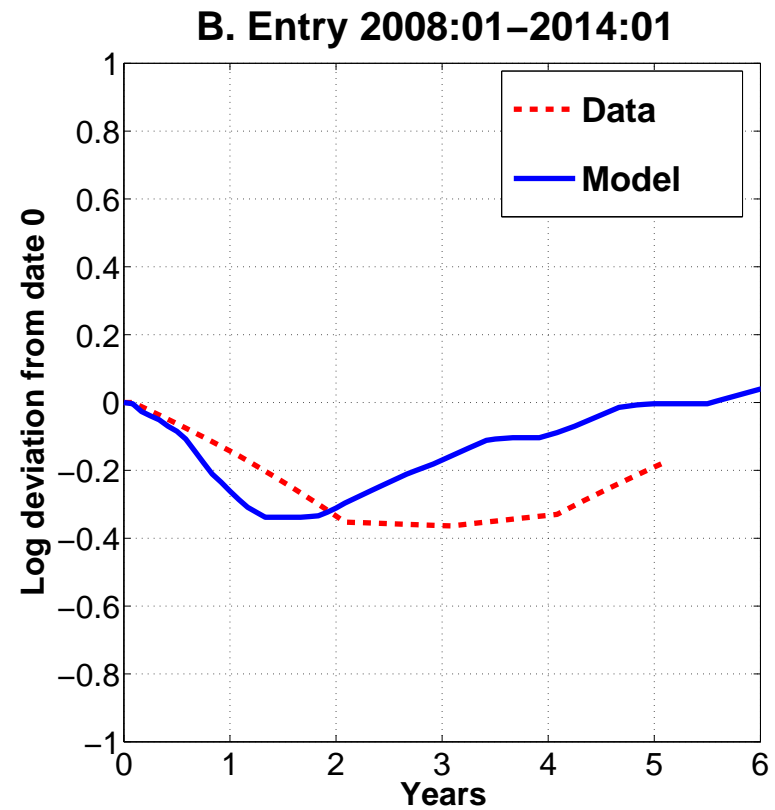
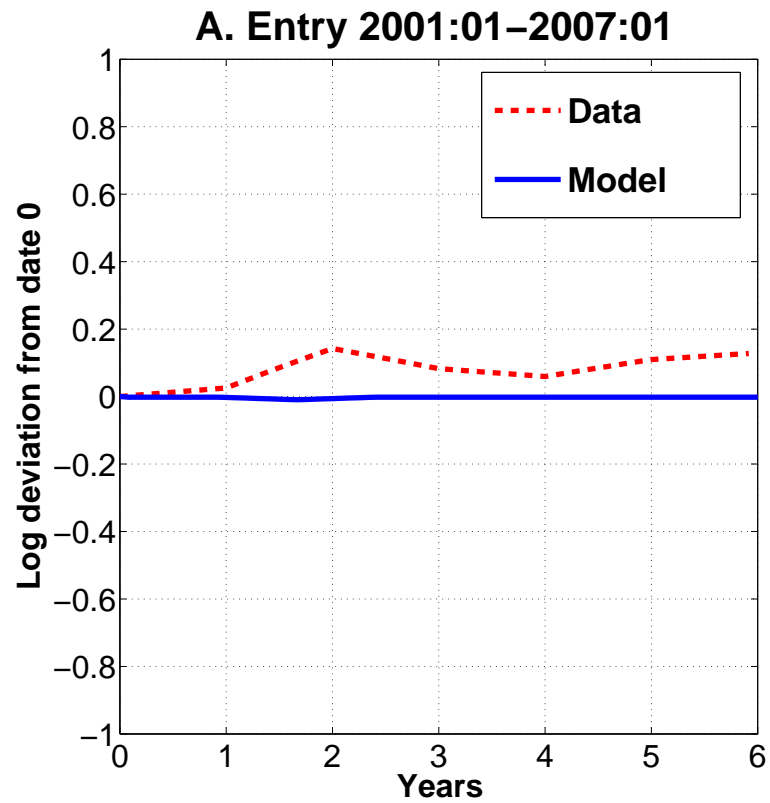
# Model: 2001 vs. 2008



B: TFP shock + fall in share of entry cost financed by equity ( $\varepsilon$ )

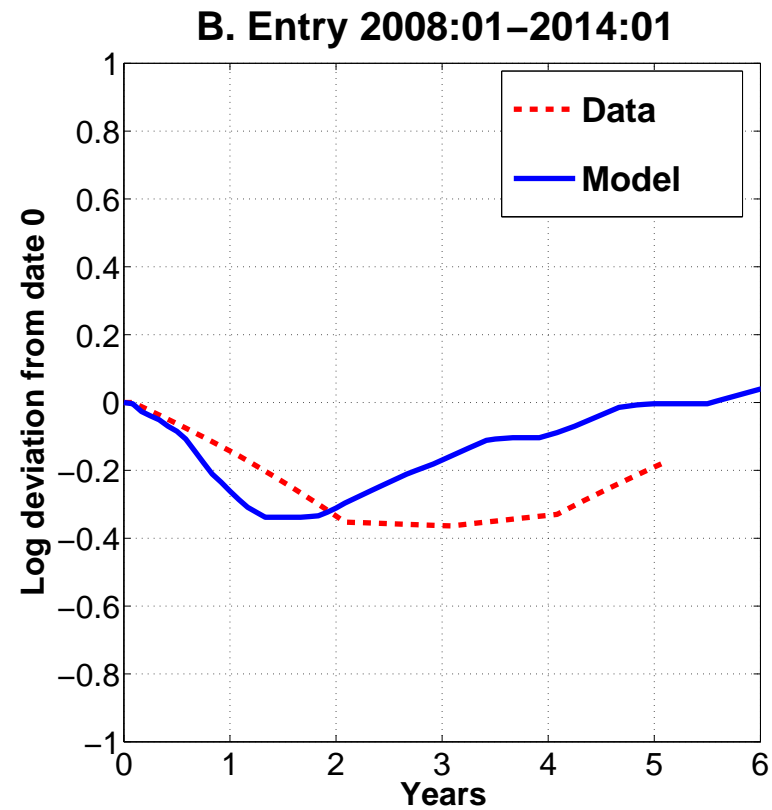
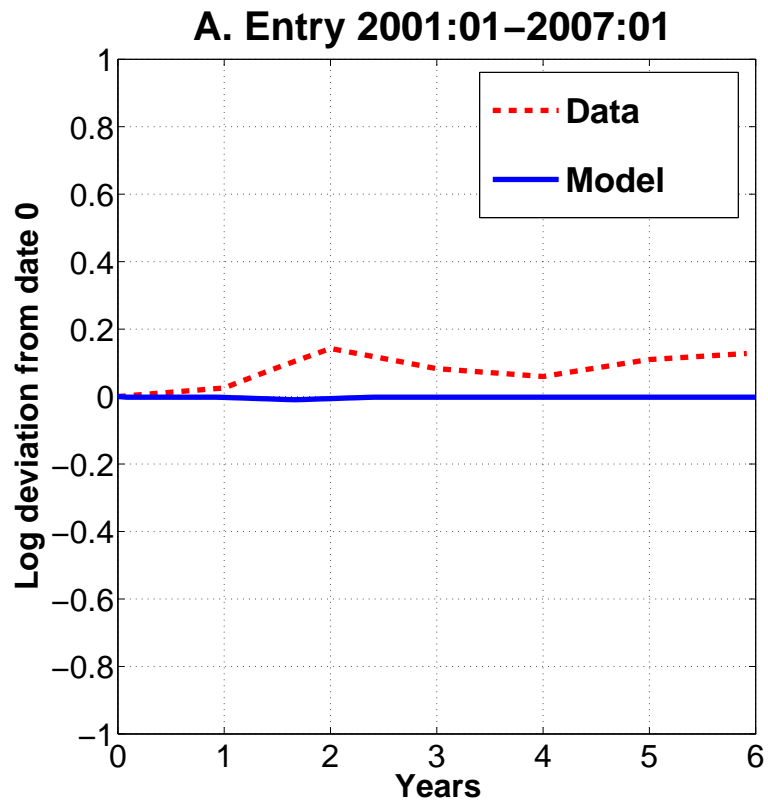


# Model: 2001 vs. 2008



A: TFP Shock

# Model: 2001 vs. 2008



B: TFP shock + fall in share of entry cost financed by equity ( $\varepsilon$ )

THANK YOU!

## State-level regressions combining HWOL ads and QWI hires

	Log Vacancy Yield		Log Vacancy Yield	
Share of Hires - Firm Age 0-1	0.233***	(0.702)	1.838**	(0.908)
Share of Hires - Firm Age 2-3	0.417	(1.648)	0.355	(1.786)
Share of Hires - Firm Age 4-5	1.434	(1.835)	1.307	(1.883)
Share of Hires - Firm Age 6-10	-0.946	(1.312)	-1.090	(1.279)
Share of Hires - Firm Size 0-19	-0.395	(0.815)	0.231	(1.231)
Share of Hires - Firm Size 20-49	0.773	(1.900)	1.428	(2.087)
Share of Hires - Firm Size 250-499	-1.330	(1.648)	-1.815	(1.789)
Share of Hires - Firm Size 500+	0.244	(0.860)	0.469	(0.935)
Constant	0.369	(0.770)	0.183	(0.818)
Observations	1,606		1,606	
R-squared	0.934		0.934	
State FE	Yes		Yes	
Quarter FE	Yes		Yes	
Seasonally Adjusted	No		Yes	

# The Christiano-Eichenbaum-Trabandt critique

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$$U_{t+1} = U_t - \Phi_t V_t^\alpha U_t^{1-\alpha} + \delta(1 - U_t)$$

- One can explain joint dynamics of  $\{U_t, V_t\}$  w/o any change in  $\Phi_t$

# The Christiano-Eichenbaum-Trabandt critique

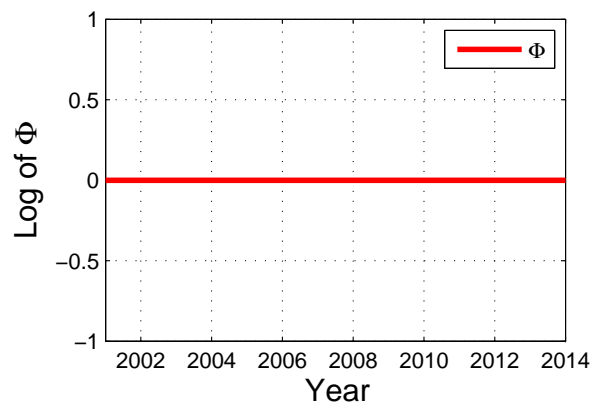
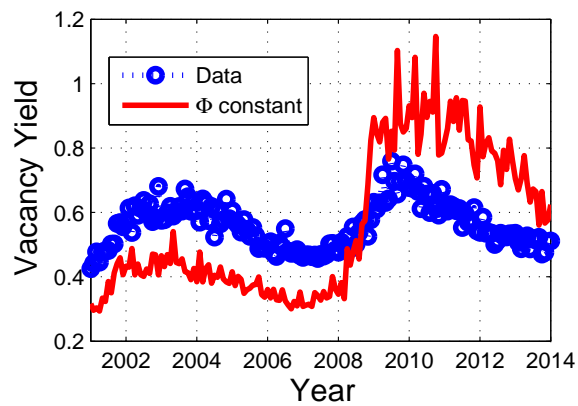
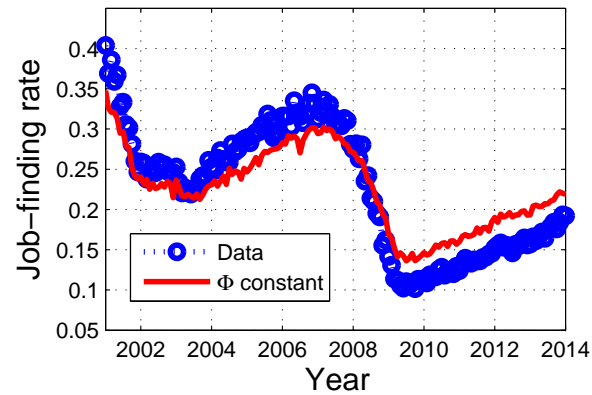
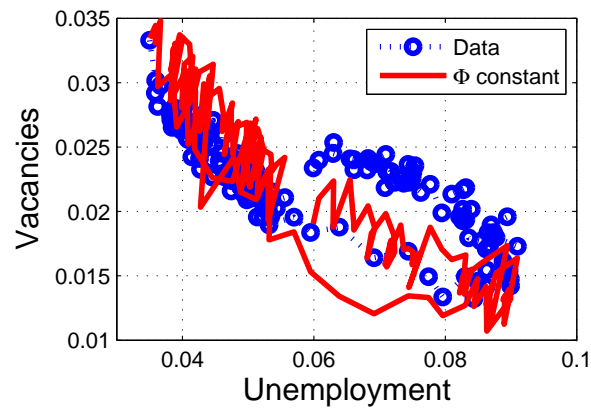
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$$U_{t+1} = U_t - \Phi_t V_t^\alpha U_t^{1-\alpha} + \delta(1 - U_t)$$

- One can explain joint dynamics of  $\{U_t, V_t\}$  w/o any change in  $\Phi_t$
- Estimation yields  $\{\hat{V}_t, \hat{H}_t\}$ , with  $\hat{H}_t = \hat{V}_t^\alpha U_t^{1-\alpha}$
- Look at model's implications for:
  1. Job-finding rate ( $\hat{H}_t/U_t$ )
  2. Vacancy yield ( $\hat{H}_t/\hat{V}_t$ )

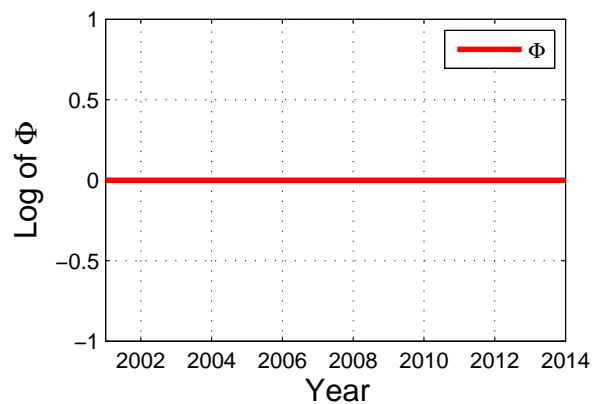
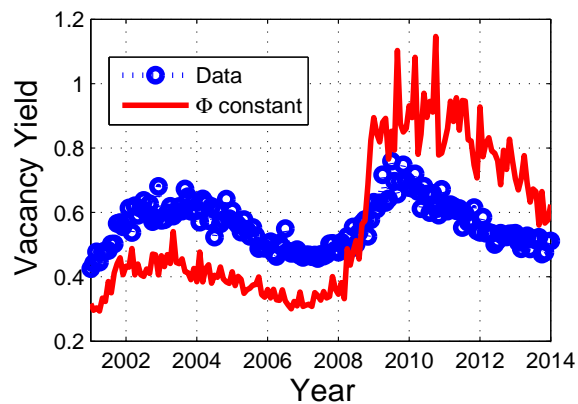
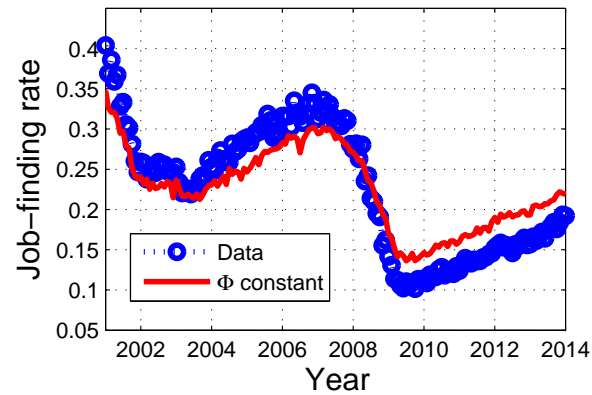
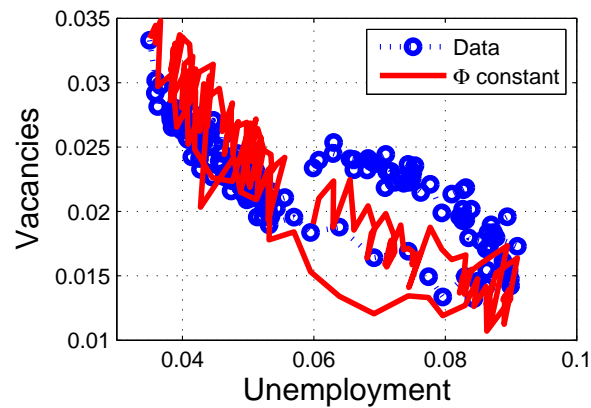
# The Christiano-Eichenbaum-Trabandt critique

- One can explain the “shift” without any change in  $\Phi_t$



# The Christiano-Eichenbaum-Trabandt critique

- One can explain the “shift” without any change in  $\Phi_t$

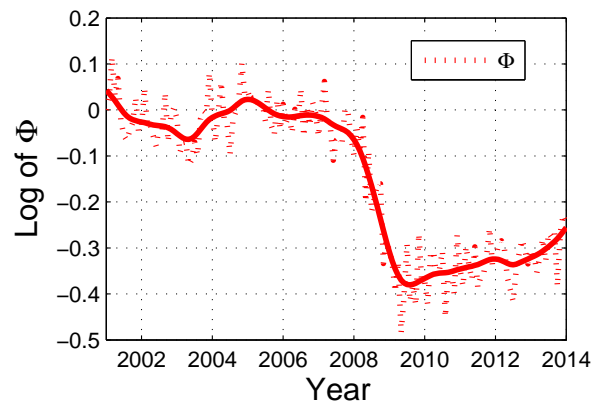
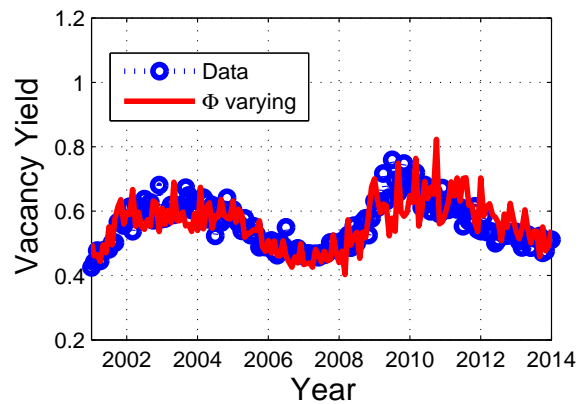
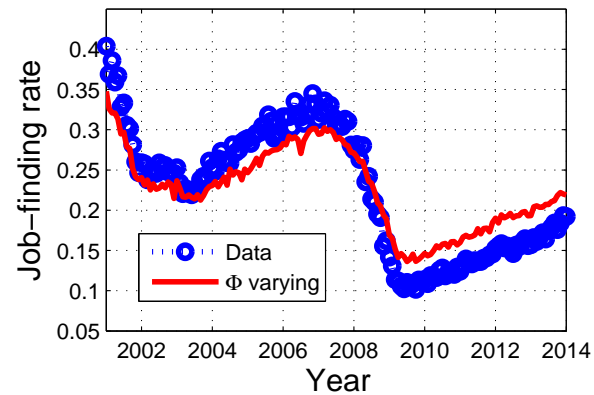
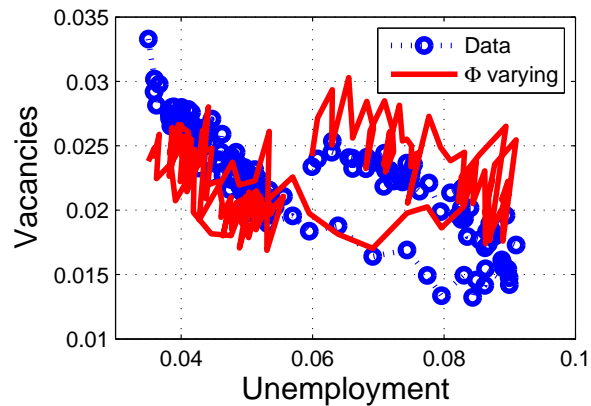


- Fit for the vacancy yield is poor



# The Christiano-Eichenbaum-Trabandt critique

- With  $\Phi_t$  time-varying:



- Fit for the vacancy yield much better